# Stata Technical Bulletin

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A publication to promote communication among Stata users

#### Editor

H. Joseph Newton Department of Statistics Texas A & M University College Station, Texas 77843 409-845-3142 409-845-3144 FAX stb@stata.com EMAIL

#### Associate Editors

Francis X. Diebold, University of Pennsylvania Joanne M. Garrett, University of North Carolina Marcello Pagano, Harvard School of Public Health James L. Powell, UC Berkeley and Princeton University J. Patrick Royston, Royal Postgraduate Medical School

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#### stata47 lookup now indexes on-line FAQs

William Gould, Stata Corporation, wgould@stata.com

There are currently about 100 FAQs totaling 300 pages available on Stata's web site and that is growing. FAQ stands for Frequently Asked Question and it is web jargon for pages recording answers to popular questions. As you can calculate for yourself from the statistics, the average FAQ runs about 3 pages. To access the FAQs,

1. point your browser to http://www.stata.com;

- 2. click on User Support;
- 3. click on FAQs.

A FAQ is a document that opens with a question and then provides the answer. For instance, one of the FAQs on Stata's web site appears as

 as

 What does "completely determined" mean in my logistic regression output?

mat uo	tes completely determined mean in my logistic regression output.			
Title: Author: Date:	Interpreting "completely determined" when running logistic William Sribney, Stata Corporation July 1996			
There are two causes for messages like				
Note:	4 failures and 0 successes completely determined			
after the commands logistic, logit, and probit. Let us deal with the most				

unlikely case first. This case occurs when ....

## This particular FAQ runs about 7 pages.

Finding the FAQ that interests you can be a daunting task. On the web site, we currently categorize FAQs according to

Questions about Windows Installation Memory allocation Crashes Printing Miscellaneous

Questions about Macintosh Installation Memory allocation Crashes Miscellaneous

Questions about Unix

Questions about Statistics Cross-sectional time-series (panel) data Logistic and probit regression Survival analysis Survey and robust estimators Estimation commands Tests Probability distributions Other commands

Questions about Programming

Questions about Data Management Reading and inputting data Combining datasets Memory usage Data manipulation Data reporting Dates Other FAQs concerning releases before Stata 5.0

To make finding the FAQs easier, we have updated the lookup database to include them.

lookup is the Stata command that indexes the Stata on-line help, the printed documentation, and now, the FAQs. Windows and Macintosh users can also access lookup by pulling down *Help* from the top menu bar.

The referenced URL http://www.stata.com/support/faqs/stat/ will take you directly to the statistics FAQ page; alternatively you could go to http://www.stata.com, click on User Support, click on FAQs, and click on Statistics. However you get to the page, from there you click on Logistic and probit regression and then you scroll down the sublist until you find the completely-determined question.

It is unlikely that you would ever think to lookup the phrase "completely determined" or that we will remember to index such a phrase, but if you type lookup logistic or lookup logit, you will find this FAQ.

#### Listing only the FAQs

Those who use Stata for Windows or Macintosh will find pulling down *Help* from the top menu bar the easier way to access lookup. A major advantage is that they can then scroll through the list.

No matter which operating system you use, however, you can use the lookup command and restrict what is listed. Typing

. lookup logistic (references to 11 manual entries omitted) (references to 11 STB inserts omitted) (references to 8 FAQs omitted)

(or pulling down *Help* and typing logistic) produces a list of 11 + 11 + 8 = 30 references. If you want just the FAQs, you can include the class(faq) option. Here are the eight FAQs relevant to logistic regression:

```
. lookup logistic, class(faq)
```

FAQ		Interpreting the cut points in ordered probit and logit
	4/97	
FAQ	  11/96	. Interpreting "outcome does not vary" when running logistic 
FAQ	  3/97	
FAQ	Compar:  8/95	ison of the nested logit and the constrained multinomial models W. Gould Is there a nested logit program for Stata? On-line FAQ at http://www.stata.com/support/faqs/stat/ Click on Logistic and probit regressions
FAQ	  7/96	Interpreting "completely determined" when running logistic 
FAQ	  3/96	A terminology problem: odds ratio versus odds W. Gould and J. Hardin Why does the manual claim that the odds ratio is constant in a logistic regression? On-line FAQ at http://www.stata.com/support/faqs/stat/ Click on Logistic and probit regressions

FAQ	Convergence of maximum-likelihood estimators
	11/96 Why does my mlogit take so long to converge? On-line FAQ at http://www.stata.com/support/faqs/stat/ Click on Logistic and probit regressions
FAQ	The appropriate command for matched case-control data
	3/96 Can I do n:1 matching with the mcc command? On-line FAQ at http://www.stata.com/support/faqs/stat/ Click on Other commands
If you wanted to obtain	in just the relevant STB inserts, you could type
. looku	p logistic, class(stb)
STB-36	<pre>sbe14 . OR's &amp; ci's for logistic reg. models with effect modification (help effmod if installed) J. Garrett 3/97 STB Reprints Vol 6, pages 104114 calculates odds ratios and confidence intervals for logistic regression models with significant interaction terms</pre>
STB-28	<pre>sbe12 Using lfit and lroc to evaluate mortality prediction models  J. M. Tilford, P. K. Roberson, and D. H. Fiser 11/95 STB Reprints Vol 5, pages 7781 discussion of how the new lfit and lroc commands (see crc41) can be used to evaluate mortality prediction models</pre>
STB-35	<pre>sg63 . Logistic regression: standardized coef. &amp; partial correlations (help lstand if installed) J. Hilbe 1/97 STB Reprints Vol 6, pages 162163 command for use after logistic; displays predictor, its coefficient, odds ratio, standardized coefficient, partial correlation, and p-value</pre>
STB-30	sg50
STB-33	sg42.1
STB-26	sg42 Plotting predicted values from linear & logistic regr. models (help regpred and logpred if installed) J. Garrett 7/95 STB Reprints Vol 5, pages 111116 calculate and plot predicted values and 95 percent confidence intervals of the predictions for one predictor holding constant the other predictors
(remainin	ng output omitted)

Actually, you can type lookup logistic, class(stb) or you can type lookup logistic, stb; typing just stb is a synonym for class(stb). For the new FAQs, however, you must type class(faq) if you wish to restrict the listing.

#### Updates

When you install the official updates from the STB, the lookup database is also updated. All STB inserts up to and including the previous issue are indexed along with all current FAQs.

stata48 Updated reshape
-------------------------

William Gould, Stata Corporation, wgould@stata.com

Below is all-new documentation on the all-new reshape command which has all-new syntax. Before you panic, we hasten to add that the new reshape command understands the old command's syntax without you specifying version numbers or anything else. It just works, both the old way and the new.

The new reshape command has a number of improvements:

- 1. The syntax is easier to specify and you need specify less.
- 2. The syntax allows variable names to be suffixed with numbers—as did the old—and it allows numbers to appear in the middle of variable names, such as inc80m and inc81m. It allows groups to be indicated by characters as well as numbers, such as incm and incf for income of males and females or even minc and finc.

- 3. The command provides better diagnostics when there are problems—including a new reshape error command for use when the data have problems. reshape error lists the problem observations.
- 4. The command checks assumptions about the data more carefully so that if there are problems, you are told ahead of time rather than after you obtain an unexpected result.
- 5. The code is structured so that the conversion process requires less free memory.
- 6. The problem reshape had with allowing only 10 constant-within-group variables is fixed.
- 7. All the improvements Weesie (1997) incorporated into his reshape2 command have been included in the new reshape.

#### **Basic syntax**

```
reshape wide varnames, i(varlist) [ j(varname [values]) other_options]
reshape long varnames, i(varlist) [ j(varname [values]) other_options]
reshape wide
reshape long
reshape error
```

where values is #[-#]  $[\#[-\#] \dots]$  and other\_options is string atwl(chars) and both are seldom specified.

## Advanced syntax

```
reshape i varlist
reshape j varname [#[-#] [#[-#] ...]] [, string]
reshape xij fvarnames [, atwl(chars) ]
reshape xi [varlist]
reshape query
reshape
reshape wide
reshape long
reshape error
reshape clear
```

where *fvarnames* are either *varnames*, *varnames* with @ characters, or a mix of the two. The @ character denotes where the #(j) suffix appears.

#### Description of basic syntax

Think of the data as a collection of observations  $X_{ij}$ . One such collection might be:

	(wide form)					(long	g form	)
-i- id	sex	inc80	X_ij inc81	inc82	-i- id	-j- year	sex	-X_ij- inc
1	0	5000	5500	6000	1	80	0	5000
2	1	2000	2200	3300	1	81	0	5500
3	0	3000	2000	1000	1	82	0	6000
					2	80	1	2000
					2	81	1	2200
					2	82	1	3300
					3	80	0	3000
					3	81	0	2000
					3	82	0	1000

reshape converts data from one form to the other:

. reshape long	inc, i(id)	j(year)	(goes from left-form to right)
. reshape wide	inc, i(id)	j(year)	(goes from right-form to left)

In this example one observation is, at least logically speaking,

+	+		in th	e long	+
1	. ]	list	if i	.d==1	1
1					1
OR		id	sex	year	inc
1	1.	1	0	80	5000
+	2.	1	0	81	5500
	3.	1	0	82	6000
	+				+
	     OR	. ]   OR     11. -+   2.	. list   0R   id   1. 1 -+   2. 1	. list if i       OR   id sex     1. 1 0 -+   2. 1 0	-+ + in the long     . list if id==1   0R   id sex year   1. 1 0 80 -+   2. 1 0 81   3. 1 0 82 +

and you want to think of this single "observation" as  $X_{ij}$ .

The i variable denotes the logical observation and is often called the group identifier. i is variable id in our data.

j denotes the subobservation and so is often called the subgroup or within-group identifier. j is year in our data, or at least, variable year when the data is in the long form. There is no j variable in the wide form. Instead, the inc variable is suffixed with the values of j, forming inc80, inc81, and inc82.

That leaves only the variable sex, which we did not specify when we typed

. reshape long inc, i(id) j(year)

or

```
. reshape wide inc, i(id) j(year)
```

Since sex is not specified, sex is assumed to be constant within i and reshape verifies that assumption before converting the data.

Here is an example with two  $X_{ij}$  variables with the data in wide form:

. list	;								
	id	sex	inc80	inc81	inc82	ue80	ue81	ue82	
1.	1	0	5000	5500	6000	0	1	0	
2.	2	1	2000	2200	3300	1	0	0	
З.	3	0	3000	2000	1000	0	0	1	

To convert this into the long form, we type

. reshape long inc ue (note: j = 80 81 82)				
Data	wide	->	long	
Number of obs.			9	
Number of variables	8	->	5	
j variable (3 values) xij variables:		->	year	
	inc80 inc81 inc82	->	inc	
	ue80 ue81 ue82	->	ue	

Note that there is no variable named year in our original, wide dataset. year will be a new variable in our long dataset. After conversion, we have

•	list					
		id	year	sex	inc	ue
	1.	1	80	0	5000	0
	2.	1	81	0	5500	1
	з.	1	82	0	6000	0
	4.	2	80	1	2000	1
	5.	2	81	1	2200	0
	6.	2	82	1	3300	0
	7.	3	80	0	3000	0
	8.	3	81	0	2000	0
	9.	3	82	0	1000	1

Similarly, if we took this dataset and typed

```
. reshape wide inc ue, i(id) j(year)
(note: j = 80 81 82)
Data
                           wide
                                -> long
    _____
Number of obs.
                             9
                                ->
                                        3
Number of variables
                             5
                                 ->
                                        8
j variable (3 values)
                           year
                                 ->
                                     (dropped)
xij variables:
                            inc
                                ->
                                     inc80 inc81 inc82
                            ue
                                 ->
                                     ue80 ue81 ue82
```

we would be right back to our original data,

. lis	t								
	id	inc80	ue80	inc81	ue81	inc82	ue82	sex	
1.	1	5000	0	5500	1	6000	0	0	
2.	2	2000	1	2200	0	3300	0	1	
з.	3	3000	0	2000	0	1000	1	0	

except for variable order.

Converting from wide to long creates the j (year) variable. Converting from long to wide drops the j (year) variable.

## **Mistakes**

The following wide data contain a mistake:

```
. list
      id
           sex
                 inc80
                         inc81
                                 inc82
          0
1
       1
                  5000
                          5500
                                  6000
 1.
 2.
                                  3300
       2
                  2000
                          2200
 з.
       3
          0
                  3000
                          2000
                                  1000
 4.
       2
            0
                  2400
                          2500
                                  2400
. reshape long inc, i(id) j(year)
(note: j = 80 81 82)
i=id does not uniquely identify the observations;
there are multiple observations with the same value of id.
Type "reshape error" for a listing of the problem observations.
r(9);
```

The *i* variable must be unique when the data are in the wide form; we said i(id) yet we have two observations for id = 2. Is person 2 a male or female?

Spotting the error in this small dataset is easy. Regardless of the size of the data, reshape error will assist us in spotting the problem. reshape error will provide assistance whenever the original error message says "type reshape error for a listing of the problem observations".

It is not a mistake when the *i* variable is repeated in long data, but the following long data have a similar kind of mistake:

```
1.
       1
              80
                      0
                           5000
  2.
              81
                      0
                           5500
        1
              82
                      0
                           6000
  з.
        1
  4.
        2
              80
                      1
                           2000
  5.
        2
              81
                     1
                           2200
  6.
        2
              82
                     1
                           3300
  7.
        3
              80
                      0
                           3000
              81
                      0
                           2000
  8.
        3
  9.
        3
              82
                      0
                           1000
 10.
        3
              82
                     0
                           1000
 reshape wide inc, i(id) j(year)
(note: j = 80 81 82)
year not unique within id;
there are multiple observations at the same year within id.
Type "reshape error" for a listing of the problem observations.
r(9);
```

inc

In the long form, i(id) does not have to be unique, but j(year) must be unique within i(); otherwise, what is the value of inc in 1981 for id = 1? As before, reshape error will assist in finding the problem:

```
. reshape error
(note: j = 80 81 82)
i (id) indicates the top-level grouping such as subject id.
j (year) indicates the subgrouping such as time.
The data are in the long form; j should be unique within i.
There are multiple observations on the same year within id.
The following 2 out of 10 observations have repeated year values:
       id
            year
  9.
       3
              82
10.
              82
        3
(data now sorted by id year)
```

Finally, consider the following (long) data which has no mistake in it:

. list	5				
	id	year	sex	inc	ue
1.	1	80	0	5000	0
2.	1	81	0	5500	1
з.	1	82	0	6000	0
4.	2	80	1	2000	1
5.	2	81	1	2200	0
6.	2	82	1	3300	0
7.	3	80	0	3000	0
8.	3	81	0	2000	0
9.	3	82	0	1000	1

What if we forget to specify ue, a variable that varies within *i*?

```
. reshape wide inc, i(id) j(year)
(note: j = 80 81 82)
ue not constant within id
Type "reshape error" for a listing of the problem observations.
r(9);
```

In this case reshape observed that ue was not constant within i and so could not restructure the data so that there were single observations on i. Of course, we should have typed reshape wide incue, i(id) j(year). We could type reshape error if the problem were not obvious.

In summary, there are three cases in which reshape will refuse to convert the data:

- 1. the data are in the wide form and *i* is not unique;
- 2. the data are in the long form and j is not unique within i;
- 3. the data are in the long form and an unmentioned variable is not constant within i.

id

year

sex

## Other mistakes

There are obviously other mistakes one might make but in such situations reshape will probably convert the data and produce a surprising result because there is no way of knowing this is not what you intend.

For instance, consider the following wide data where we forget to mention that variable ue varies within id:

. list	5								
	id	sex	inc80	inc81	inc82	ue80	ue81	ue82	
1.	1	0	5000	5500	6000	0	1	0	
2.	2	1	2000	2200	3300	1	0	0	
з.	3	0	3000	2000	1000	0	0	1	
		long in = 80 81		) j(year)	wide	->	long		
Number	of	obs.					g	· · )	 
Number	c of	variabl	es		8	->	7		
j vari xij va		(3 val les:	ues)			->	year		
2									

reshape does not complain but here is the result:

. list

	id	year	sex	ue80	ue81	ue82	inc
1.	1	80	0	0	1	0	5000
2.	1	81	0	0	1	0	5500
з.	1	82	0	0	1	0	6000
4.	2	80	1	1	0	0	2000
5.	2	81	1	1	0	0	2200
6.	2	82	1	1	0	0	3300
7.	3	80	0	0	0	1	3000
8.	3	81	0	0	0	1	2000
9.	3	82	0	0	0	1	1000

We did not state that ue varied within i and so the variables ue80, ue81, and ue82 were left as-is. There is no real problem here because no information has been lost. In fact, this may be the result we wanted.

Probably, however, we simply forgot to include ue among the  $X_{ij}$  variables. If you obtain an unanticipated result here is how to undo it:

If you typed 'reshape long...' to produce it, type reshape wide (without arguments) to undo it.

If you typed 'reshape wide ...' to produce it, type reshape long (without arguments) to undo it.

So we can type reshape wide to get back to our original data and then type the reshape long command we intended: reshape long inc ue, i(id) j(year).

## reshape long and reshape wide without arguments

Whenever you type a reshape long or reshape wide command with arguments, reshape remembers it. Thus you might

```
. reshape long inc ue, i(id) j(year)
```

and work with the data like that. You could then type

. reshape wide

to convert it back to the wide form. You might do some more work. You could type

. reshape long

to convert it back to the long form. If you save the data, you can even continue using reshape wide and reshape long without arguments the next day.

Be a little careful, however. If you create new  $X_{ij}$  variables, you must tell reshape about them by typing out the full reshape command, although no real damage will be done if you forget. If you are converting from long to wide, reshape itself will catch your error and refuse to do the conversion. If you are converting from wide to long, reshape will convert the data, but the result will be surprising (remember what happened when we forget to mention variable ue and ended up with ue80, ue81, and ue82 in our long data). You can 'reshape long' to undo it and then try again.

## **Missing variables**

When converting data from the wide to the long forms, reshape does not demand that all the variables exist. Missing variables are treated like variables with missing observations. For instance, consider

list

	id	sex	inc80	inc81	inc82	ue80	ue82
1.	1	0	5000	5500	6000	0	0
2.	2	1	2000	2200	3300	1	0
З.	3	0	3000	2000	1000	0	1

Note that variable ue81 is missing. We can still type

```
. reshape long inc ue, i(id) j(year)
(note: j = 80 81 82)
(note: ue81 not found)
Data
                                     -> long
                                wide
  _____
                                               9
Number of obs.
                                   3
                                      ->
                                               5
Number of variables
                                   7
                                      ->
j variable (3 values)
                                      ->
                                           year
xij variables:
                    inc80 inc81 inc82
                                      ->
                                           inc
                      ue80 ue81 ue82
                                      ->
                                           ue
```

The result is

. list, nodisplay

	id	year	sex	inc	ue
1.	1	80	0	5000	0
2.	1	81	0	5500	
з.	1	82	0	6000	0
4.	2	80	1	2000	1
5.	2	81	1	2200	
6.	2	82	1	3300	0
7.	3	80	0	3000	0
8.	3	81	0	2000	
9.	3	82	0	1000	1

Were we to reshape these data back to the wide form by typing reshape wide incue, i(id) j(year), the variable ue81 would be created and it would contain all missing values.

## Advanced issues with basic syntax: i()

The syntax is

reshape ..., i(*i\_variable*) ... or reshape ..., i(*i\_variables*) ...

Typically *i* is one variable—such as subject id—but it could be multiple variables such as hospital id and hospital's patient id.

Examples include

reshape ..., i(id)
reshape ..., i(hid pid)

## Advanced issues with basic syntax: j()

The syntax is

reshape ..., ... j(*j\_variable*) ... or reshape ..., ... j(*j\_variable j\_values*) ...

The second syntax defines the j variable and its values. When you leave the values unspecified, reshape works them out for itself.

reshape never makes a mistake when the data is in long form—when you type reshape wide. The values can easily be obtained by tabulating the existing j variable.

reshape can make a mistake when your data is in the wide form—when you type reshape long—if you have named your variables poorly. Pretend you have the variables inc80, inc81, and inc82, recording income in each of the indicated years, and you have a variable named inc2, which is not income but when the area was reincorporated. You type

. reshape long inc, i(id) j(year)

reshape would see the variables inc2, inc80, inc81, and inc82 and decide that there are four groups: j = 2, 80, 81, and 82. The best way to address such problems is to name your variables appropriately. The date of reincorporation would be better named something other than inc followed by a number; reinc would be a good name.

Alternatively, you can keep the name and specify the *j* values. To perform the reshape, you would type

```
. reshape long inc, i(id) j(year 80-82)
```

or

```
. reshape long inc, i(id) j(year 80 81 82)
```

The dash notation for ranges can be mixed with individual numbers. reshape would understand 80 82-87 89 91-95.

At the other extreme, you can omit the j() option altogether. If you do, reshape long will name the j variable  $_j$  and reshape wide will assume the variable is named  $_j$ .

## Advanced issues with basic syntax: X\_ij

When specifying the variable names you may include @ characters to indicate where the numbers go. For instance, in the following data

list	;								
	id	sex	inc80r	inc81r	inc82r	ue80	ue81	ue82	
1.	1	0	5000	5500	6000	0	1	0	
2.	2	1	2000	2200	3300	1	0	0	
З.	3	0	3000	2000	1000	0	0	1	

you would type

```
reshape long inc@r ue, i(id) j(year)
(note: j = 80 81 82)
Data
                                         -> long
                                  wide
       _____
                                        _ _ _ _
Number of obs.
                                                  9
                                     3
                                         ->
Number of variables
                                     8
                                        ->
                                                  5
j variable (3 values)
                                         ->
                                             year
xij variables:
                  inc80r inc81r inc82r
                                         ->
                                              incr
                       ue80 ue81 ue82
                                         ->
                                             ue
```

At most one @ character may appear in each name. If no @ character appears, results are as if the @ character appeared at the end of the name. So equivalent to the above is

. reshape long inc@r ue@, i(id) j(year)

Either way, the result of the reshape long will be

. list	t				
	id	year	sex	incr	ue
1.	1	80	0	5000	0
2.	1	81	0	5500	1
з.	1	82	0	6000	0
(output	omitte	ed)			
9.	3	82	0	1000	1

That is, inc@r specifies variables named inc#r in the wide format and incr in the long.

The @ notation may similarly be used for converting long to wide datasets:

```
. reshape wide inc@r ue, i(id) j(year)
(output omitted)
```

#### Advanced issues with basic syntax: the atwl() option

Option atwl() is for use when @ characters are also specified:

reshape varnames\_with\_0, ... atwl(chars)

atwl() stands for at-when-long. When you specify a name such as inc@r or ue@ in the long form, the name becomes incr and ue; the @ character is changed into nothing. atwl() lets you change it into something.

If you specify atwl(X), the long-form names would become incXr and ueX. If you specified atwl(yr), the long-form names would become incyrr and ueyr.

atwl() is seldom specified.

## Advanced issues with basic syntax: string identifiers for j()

The string option allows j to take on string values:

reshape ..., ... string

For instance, consider the following wide data on husbands and wives:

list				
	id	kids	incm	incf
1.	101	0	5000	5500
2.	102	2	2000	2200
3.	103	1	3000	2000

In this data, incm is the income of the man and incf the income of the woman. This data can be reshaped into separate observations for males and females by typing

<pre>. reshape long inc, i(id) (note: j = f m)</pre>	j(sex) string			
Data	wide	->	long	
Number of obs.	3	->	6	
Number of variables	4	->	4	
j variable (2 values) xij variables:		->	sex	
	incf incm	->	inc	

The string option specifies that j will take on nonnumeric values. The result is

. list id sex kids inc 1. 101 0 5500 f 5000 2. 101 m 0 з. 102 2200 f 2 102 2 2000 4. m 5. 103 f 1 2000 6. 103 1 3000 m

sex will be a string variable. Similarly, these data can be converted from long to wide by typing

<pre>. reshape wide inc, i(id) j (note: j = f m)</pre>	(sex) string			
Data	wide	->	long	
Number of obs.			3	
Number of variables	4	->	4	
j variable (2 values) xij variables:	sex	->	(dropped)	
	inc	->	incf incm	

Strings are not limited to being single characters or even of the same length. Had the original data been

•	list				
		id	kids	incmale	incfem
	1.	101	0	5000	5500
	2.	102	2	2000	2200
	з.	103	1	3000	2000

then reshape long inc, i(id) j(sex) string would have resulted in

. lis	t			
	id	sex	kids	inc
1.	101	fem	0	5500
2.	101	male	0	5000
з.	102	fem	2	2200
4.	102	male	2	2000
5.	103	fem	1	2000
6.	103	male	1	3000

Where the string identifier appears may be specified using the @ notation. In the following wide data, the m and f appear as a prefix rather than a suffix:

. list

id	kids	minc	finc
101	0	5000	5500
102	2	2000	2200
103	1	3000	2000
	101 102	101 0 102 2	101         0         5000           102         2         2000

The reshape command is

. reshape long @inc, i(id) j(sex) string (output omitted)

The resulting variable in the long format will be named inc.

Just as with numbers, strings may be placed in the middle. If the variables are named incMome and incFome, the reshape command would be

. reshape long inc@ome, i(id) j(sex) string
(output omitted)

Be careful with string identifiers because it is easy to be surprised by the result. Consider a person with wide data having variables named incm, incf, uem, uef, and agem, agef. To make the data long, the person types

. reshape long inc ue age, i(id) j(sex) string

Along with these variables, the person innocently has the variable agenda. reshape will decide the sexes are m, f, and nda. This would not happen without the string option if the variables were named inc0, inc1, ue0, ue1, and age0, age1 even with variable agenda present in the data.

## Advanced issues with basic syntax: second-level nesting

You have data from a household survey of the income of husbands and wives. There are four ways these data might be organized.

They might be organized in the long-long form

	hid	sex	year	inc
1.	107	m	90	4500
2.	107	f	90	3200
з.	107	m	91	4600
4.	107	f	91	4700
3.	107	f m	91	46

or in the long-year wide-sex form

	hid	year	finc	minc
1.	107	90	3200	4500
2.	107	91	4700	4600

or in the wide-year long-sex form

	hid	sex	inc90	inc91
1.	107	f	3200	4700
2.	107	m	4500	4600

or the wide-wide form

	hid	finc90	minc90	finc91	minc91
1.	107	3200	4500	4700	4600

reshape can convert any of these forms to any other. Converting all the way from the long-long form to the wide-wide form (or from the wide-wide form to the long-long) requires two reshape commands.

Starting in the wide-wide form, we can convert to (say) the long-year wide-sex form by typing

. reshape wide @inc, i(hid year) j(sex) string

This in turn can be converted to the wide-wide form by typing

. reshape wide minc finc, i(hid) j(year)

We can go back from the wide-wide to the long-long by repeating the two steps in reverse order:

reshape long minc finc, i(hid) j(year)
reshape long @inc, i(hid year) j(sex) string

Pairs of reshape commands can result in remarkable dataset transformations. For instance, you can convert

	gid	year	rs1	rs2	rs3	sex
1.	26	90	57	28	30	m
2.	26	91	52	33	32	m

sex	rs91	rs90	visit	gid	
m	52	57	1	26	1.
m	33	28	2	26	2.
m	32	30	3	26	З.

by typing

into

. reshape long rs, id(gid year) j(visit) . reshape wide rs, id(gid visit) j(year)

## **Description of advanced syntax**

The advanced syntax is simply a different way of specifying the reshape command and it has one seldom-used feature providing a little extra control. Rather than typing a single reshape command to describe the data and perform the conversion, such as

. reshape long inc, i(id) j(year)

you type a sequence of reshape commands. The initial commands describe the data and the last performs the conversion:

```
reshape i id
reshape j year
reshape xij inc
reshape long
```

reshape i corresponds to i() in the basic syntax.

reshape j corresponds to j() in the basic syntax.

reshape xij corresponds to the variables specified in the basic syntax.

In addition, there is one more specification which has no counterpart in the basic syntax:

#### reshape xi varlist

In the basic syntax, all unspecified variables are assumed to be constant within *i*. The advanced syntax works the same way unless you specify the reshape xi command. reshape xi names the constant-within-*i* variables. If you specify reshape xi, then any variables that are not explicitly specified are dropped from the data during the conversion.

As a practical matter, it would probably be better if you explicitly dropped the unwanted variables before conversion. For instance, imagine the data have variables inc80, inc81, inc82, sex, age, and age2 and that you no longer want the age2 variable. You could specify

. reshape xi sex age

or you could

. drop age2

and leave reshape xi unspecified. reshape xi does have one minor advantage: It saves reshape from going to the work of determining which variables are unspecified. This saves a relatively small amount of computer time.

Another advanced-syntax feature is reshape query—equivalent to typing reshape by itself. reshape query presents a report on what has been defined:

Xij	Command/contents
Subscript i,j definitions: group id variable(s) within-group variable and its range	   reshape i hid   reshape j year 
Variable X definitions: varying within group constant within group (opt)	1 0

Optionally type "reshape xi" to define variables that are constant within i. Type "reshape long" to convert the data to long form.

reshape i, reshape j, reshape xij, and reshape xi specifications may be given in any order and may be regiven to change or correct what has been specified.

Finally, reshape clear clears the definitions. Remember that reshape definitions are stored with the dataset when you save it. reshape clear provides a way to erase the definitions if you do not want this.

The basic syntax of reshape is implemented in terms of the advanced syntax. That means you can mix basic and advanced syntaxes.

The syntax of the prior version of reshape was

reshape cons *varname* [*varname* ...]

reshape groups groupvar #[-#] [#[-#] ...]

reshape vars *varname varname* ...

reshape query

reshape wide

reshape long

You may continue to use the old syntax; the new reshape understands that. The new syntax is, however, better.

Here is the mapping between old and new syntax:

old syntax		new synta	X
reshape cons reshape grou reshape vars	ıps	reshape reshape reshape	j
reshape quer reshape wide reshape long		reshape reshape reshape	wide

In the old reshape cons command you specified the identification variables and any variables that were constant within group. The new way to do that is

reshape i *identification\_variables* 

reshape xi constant\_within\_group\_variables

and then, it would better if you left the *constant\_within\_group\_variables* unspecified because the new reshape can figure that out for itself. If you specify the list, you are likely to forget a variable or two.

In addition, the old reshape cons command was limited to 10 variables. The new reshape i is also limited to 10 variables, but the constraint does not matter because it will certainly not take that many variables to identify the groups and the constant-withingroup variables are specified either with the reshape xi command or left unspecified. There is now no limit as to the number of constant-within-group variables (explicitly specified or implied).

The new reshape uses less memory and is slightly faster once it gets going; it spends more time thinking about what it is going to do, however. The new reshape has better error checking—especially for data problems such as nonunique id variables that might otherwise go undiscovered. All those advantages accrue whether you use the old or new syntax.

## Acknowledgment

We would like to thank Jeroen Weesie of Utrecht University for his reshape2 command (Weesie 1997), the ideas of which were incorporated into this version of reshape.

## Saved results

So that reshape long and reshape wide can be given without arguments, reshape stores the following characteristics with the data:

\_dta[ReS\_ver] v.1 if old-syntax commands were used v.2 if new-syntax commands were used \_dta[ReS\_i] *i* variable name(s) j variable name \_dta[ReS\_j] \_dta[ReS\_jv] j values if specified \_dta[ReS\_Xij]  $X_i j$  variable name(s) \_dta[ReS\_Xi]  $X_i$  variable name(s) if specified \_dta[ReS\_atwl] atwl() value if specified \_dta[ReS\_str] 1 if option string specified; otherwise 0.

#### References

Weesie, J. 1997. dm48: An enhancement of reshape. Stata Technical Bulletin 38: 2-4.

dm49 Some new matrix commands
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Jeroen Weesie, Utrecht University, Netherlands, weesie@weesie.fsw.ruu.nl

This insert describes a collection of new matrix commands for Stata. Most of these commands operate on "explicit" Stata matrix objects. In my work, I frequently encounter situations in which I want to know some "linear algebra" property of a collection of variables. For example, "What is the matrix rank of these variables?" We might also ask "How many linear relationships exist between these variables and what are they?" Forming a matrix with mkmat is laborious and only possible with small datasets. Thus, I wrote additional "interface" programs that operate on "implicit matrices" formed by variables and row selection with standard if and in syntax.

In this insert, I do not seek to explicate linear algebra concepts, numerical linear algebra, and the applications of linear algebra in statistics. Rather, the reader should refer to the references.

Finally, I stayed away from implementing one of the most curious omissions in Stata: A linear equation solver. Stata's high-level interpreted language is simply too slow.

#### Contents

The matrix-oriented programs provided with this insert include (see help for matfunc for interactive help):

matginv	Moore–Penrose generalized-inverse
matrank	rank (number of independent rows/columns)
matcond	condition number
matorth	orthogonal basis of column space (image)
matnull	orthogonal basis of null space
matnorm	L2-norm of a matrix
matsum	row/column/overall sum
matmax	row/column/overall maximum
matmin	row/column/overall minimum
matrand	random matrix

The variable-oriented programs provided with this insert include (see help for varfunc for interactive help):

varcond	condition number of implied matrix
varrank	rank of implied matrix
varorth	Gram–Schmidt orthogonalization of variables
varnull	"null space" of variables

The matrix-oriented commands share a number of features:

- 1. They accept valid matrix expressions such as the name of a matrix, the sum of two matrices, the inverse of a matrix, and so on. Note that Stata currently does not support more general matrix expressions such as inv(X'X).
- 2. If names for output are not specified, the output is displayed.

#### Matrix functions based on the singular value decomposition

matginv matname [, ginv(name\_matrix) rank(name\_scalar) tol(#) display format(fmt)]

returns the Moore-Penrose (MP) inverse of the *matname* in a matrix named in ginv. The scalar named in rank returns the rank of *matname*. If A is a  $(n \times m)$  matrix, its MP-inverse B is  $(m \times n)$ , and is the unique solution of 1) ABA = A, 2) BAB = B, and 3) AB and BA are orthogonal projections. If A is square and regular, the MP-inverse is the ordinary matrix inverse. If A is square and singular, Stata's matrix function syminv() returns a g-inverse, which is a different kind of generalized matrix inverse. The row (column) names of the MP-inverse are the column (row) names of *matname*. See Campbell and Meyer (1979) for details on the applications of g-inverse in statistics, difference equations, and so on.

matcond matname [, <u>c</u>ond(name\_scalar) <u>d</u>isplay <u>f</u>ormat(fmt)]

returns the condition number (ratio of largest and smallest singular value) of a matrix in the scalar named in cond.

```
matrank matname [, <u>rank(name_scalar)</u> <u>display tol(#) format(fmt)</u>]
```

returns the rank (number of independent rows or columns) of a matrix in the scalar named in rank.

```
matorth matname [, orth(name_matrix) rank(name_scalar) display tol(#) format(fmt)]
```

returns an orthogonal basis of the column space (image) of a matrix in the matrix named in orth, and the rank of the matrix in the scalar named in rank.

matnull matname [, <u>null(name\_matrix)</u> <u>rank(name\_scalar)</u> <u>d</u>isplay <u>t</u>ol(#) <u>f</u>ormat(fmt)]

returns an orthogonal basis of the null space of a matrix in the matrix named in null, and the rank of the matrix in the scalar named in rank.

## Other matrix functions

```
matnorm matname [, <u>n</u>orm(name_scalar) <u>d</u>isplay <u>f</u>ormat(fmt)]
```

returns the L2-norm of a matrix in the scalar named in norm.

matmax	matname	[,	<u>r</u> ow( <i>rmatname</i> )	<u>c</u> olumn( <i>cmatname</i> )	<u>a</u> ll( <i>amatname</i> )	<u>d</u> isplay	<u>f</u> ormat( <i>fmt</i> )]	
matmin	matname	[,	<u>r</u> ow( <i>rmatname</i> )	<u>c</u> olumn( <i>cmatname</i> )	<u>a</u> ll( <i>amatname</i> )	<u>d</u> isplay	<u>f</u> ormat( <i>fmt</i> )]	
matsum	matname	[,	<u>r</u> ow( <i>rmatname</i> )	<u>c</u> olumn( <i>cmatname</i> )	<u>a</u> ll( <i>amatname</i> )	<u>d</u> isplay	<u>f</u> ormat( <i>fmt</i> )	

compute and/or display the row-wise, column-wise and over-all maximum, minimum, and sum over the elements of a matrix. More than one operator may be specified simultaneously and the result of each applied operator is placed in the matrix named in the row, column, and all options. These commands default to the column-wise operators.

matrand  $n m matname \left[, \left\{ \underline{n} \operatorname{ormal}(mn var) \mid \underline{u} \operatorname{niform}(lo hi) \mid \underline{c} \operatorname{onst}(lo hi) \right\} \underline{d} \operatorname{isplay} \underline{f} \operatorname{ormat}(fmt) \right]$ 

creates an  $(n \times m)$  matrix (overwriting the named matrix if it already exists) with elements generated independently from

normal	distribution with mean mn and variance var
uniform	distribution on the interval [lo, hi]
const	distribution on the constants $lo, lo+1, \ldots, hi$

If no distribution is specified, matrand defaults to the U(0,1) distribution.

## Options for matrix-oriented programs

display specifies that the computed results are displayed. All programs that are described here display the results if output names for matrices (scalars) are not specified.

format (fmt) specifies a format (e.g., %10.5f, %10.0g) to display matrix results.

tol (#) specifies the tolerance for deciding what singular values are 'really' zero. See below for details. You typically don't have to set this option.

#### Numerical details

The main tool used by these programs is the singular value decomposition of the matrix A = USV', where U and V are (column) orthonormal and S is diagonal with positive entries. We heavily lean on Stata's singular value decomposition command

(matrix svd). Note that Stata can only compute the "economy" solution, and hence cannot be used directly to obtain the null space of a matrix.

Following Matlab, we compute the rank r(A) of A as the number of singular values that exceed to1, where

tol = max(singular values of A) \* size(A) \* eps

where eps is a measure of machine precision.

This is also used in computing the MP-inverse (see below) and the column orthogonalization. The condition number c(A) of A is

 $c(A) = \max(\text{singular values of } A) / \min(\text{singular values of } A)$ 

If the minimum of the singular values is 0, the condition number is defined as missing.

The MP-inverse of a matrix is computed as V \* IS \* U, where IS is a diagonal matrix with the reciprocal of the singular values S, or 0 if the singular values are smaller than tol (see above).

## Examples

. matrand 5 3 A	(random matrix A, iid U(0,1))
. matrand 5 7 B, n(0 10)	(random matrix B, iid N(0,1))
. matginv A	(display Moore–Penrose inverse)
. matginv A, ginv(AI)	(return Moore–Penrose inverse)
. matcond A+B	(display condition number of $A+B$ )
. matrank A, rank(ra)	(return rank of matrix A)
. matsum A, row(rsumA)	(return row-wise sum of A)

#### Details on variable-oriented programs

These programs return linear algebra characteristics of data, i.e., of an "implied matrix" with the variables in a *varlist* as columns, and with the (if/in selected) cases without missing values as the rows. All programs make it easy to append a variable consisting of all 1's to *varlist*.

#### Description

varcond computes the condition number (ratio of largest to smallest singular values) of the implied matrix.

varrank computes the rank (number of independent columns or rows) of the implied matrix.

varorth computes a series of orthogonal variables that span the same column space as varlist by Gram-Schmidt orthogonalization.

varnull computes the "null space" of the implied matrix, i.e., a matrix of coefficients of linear dependencies between the variables.

## Options

- cons specifies that a constant variable consisting of 1's should be appended to the varlist. In varorth, the constant is prepended to the varlist, so that the generated variables are orthogonal to 1.
- display specifies that the computed characteristics should be displayed. Recall that the programs automatically display results if no names for the results are provided.

format (fmt) specifies a format (e.g., %10.4f) used to display scalars or matrices.

## **Options for varorth**

prefix(str) specifies the string prefixed to the variables in varlist to obtain the names of orthogonalized variables.

- norm specifies that the returned variables are normalized, i.e., have unit length. The (weighted) covariance matrix of orthonormalized variables is a unity matrix.
- eps(#) specifies a tolerance to decide whether a variable is linear dependent on the previous variables in the *varlist*. A more reliable way to obtain the number of linear dependencies is via varrank.

## Examples

. varrank price weight turr	(rank of data matrix with 3 columns)
. varrank price weight turr (scalarr will contai	if foreign, cons rank(r) n rank of foreign data matrix with 4 columns)
. varorth x1 x2 x3 x4	(Gram-Schmidt orthogonalization of x1-x4)
. for 1-4, l(num) : gen I@ . varorth I*	= inc <sup>°</sup> @ (polynomials in inc) (orthogonalize them)
. gen pw = price + weight . varnull price weight pw	(silly, but ok for illustration) (varnull will show a matrix with coefficients that) (indicate that pw is the sum of price and weight)

## **Technical details**

The programs varcond, varrank, varorth, and varnull are variable-oriented versions of the matrix-oriented commands matcond, matrank, matorth, and matnull. It is important to understand that the variable-oriented and the matrix-oriented programs use different algorithms. The listed matrix-functions base their results on the singular value decomposition (SVD) of a matrix (using matrix svd). The SVD provides a numerically reliable algorithm for these functions, though slower than algorithms based on, e.g., the QR decomposition. However, the SVD may require much more memory than Stata's matrix modules can cope with. Thus, the variable-oriented versions are provided as low-precision alternatives. If you fear that your data are ill-conditioned, you have enough memory, and the number of cases does not exceed matsize, you should use mkmat to make a matrix from your data and use the matrix programs.

varrank counts the number of nonzero eigenvalues of X'X (or X'WX if weights are specified) based on the spectral decomposition (matrix symeigen).

varcond computes the condition number of the variables as the square root of the ratio of the largest to smallest eigenvalues of X'X (or X'WX).

varorth uses Gram-Schmidt orthogonalization rather than the SVD of the set of orthogonal variables.

varnull returns the eigenspace of X'X (or X'WX) associated with zero (or small) eigenvalues, obtained from the spectral decomposition.

## References

Belsey, D. A., E. Kuh, and R. E. Welsch. 1980. Regression Diagnostics. Identifying Influential Data and Sources of Collinearity. New York: John Wiley & Sons.

Campbell, S. L. and C. D. Meyer, Jr. 1979. Generalized Inverses of Linear Transformations. London: Pitman.

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The MathWorks. Matlab Reference Manual. V4. Cambridge, MA: The MathWorks, Inc.

ip19	Using expressions in Stata commands
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Jeroen Weesie, Utrecht University, Netherlands, weesie@weesie.fsw.ruu.nl

On numerous occasions, I wondered why Stata does not support a list of expressions (e.g., the log-transform of a variable; the sum of variables) in place of a list of variables. Currently, one has to generate "temporary" variables manually. Support for expressions where Stata now permits variables only, was requested a number of times by other Stata users on the Stata discussion list. In this insert, I describe two programs that add support for "expression expansion" in "regular" Stata commands, that is, commands satisfying the syntax

command [varlist] [if exp] [in range] [, options]

Examples of regular commands are the descriptive commands summarize and tab and the single-equation estimation commands regress, logistic, and stcox. Some new commands such as heckman and mvreg do not support equations.

#### Syntax

expr is a prefix command that enables expressions in regular commands.

```
expr [, nodetail ]: cmd expression_list [if exp] [in range] [weight] [using filename] [, cmd_options]
exprcmd [, nodetail ]
```

An *expression\_list*, is a list of expressions, separated by one or more blanks. Thus, expressions may *not* contain embedded spaces as expr is not smart enough to parse such expressions. In addition, a variable list is interpreted as a list of "atomic" expressions, namely the untransformed existing variables.

Expression expansion is limited to the part of the input string prior to the first comma. Thus expression expansion does not involve options, equations, etc.

expr silently generates variables (of the default type, thus they are of type float if you haven't changed the default type; doing so is very dangerous anyway) named \_Expr0, \_Expr1, and so on. Any existing variables that fit the mask \_Expr are silently dropped. The generated variables are labeled using the defining expressions.

#### Example

We illustrate expr with the automobile data distributed with Stata. We want to see summary statistics of the log price and log weight of cars. For comparison, we also include the untransformed variables price and weight:

```
. expr: summ price ln(price) weight ln(weight)
Expression _Expr0 := ln(price)
Expression _Expr1 := ln(weight)
-> summ price _Expr0 weight _Expr1
Variable
               Obs
                          Mean
                                 Std. Dev.
                                                  Min
                                                             Max
               ----
  price
                      6165.257
                                 2949.496
                                                 3291
                                                           15906
                74
  _Expr0
                74
                      8.640633
                                  .3921059
                                            8.098947
                                                        9.674452
  weight
                74
                      3019.459
                                  777.1936
                                                 1760
                                                            4840
                      7.978751
  _Expr1
                74
                                 .2663436
                                            7.473069
                                                         8.48467
```

Note that expr displays the meanings (defining expressions) of the variables that are defined as expressions.

The command expr can also be used to include transformed variables in linear (linear-form) models. Thus, to include the log price of a car as a predictor of its energy preservation, one can issue the command

. expr: reg mpg ln(price) weight foreign Expression _Expr0 := ln(price) -> reg mpg _Expr0 weight foreign								
Source		df	MS		Number of obs = 74			
Model	824.162842	3 539	.765539		F(3, 70) = 45.84 Prob > F = 0.0000 R-squared = 0.6627 Adj R-squared = 0.6483	С 7		
Total	2443.45946		4720474		$\begin{array}{rcl} \text{Adj } \text{K-squared} &= & 0.0483\\ \text{Root } \text{MSE} &= & 3.4313 \end{array}$			
mpg	Coef.				[95% Conf. Interval]	-   -		
_Expr0	0419323	1.523501	-0.028	0.978	-3.08046 2.996595	5		
weight	0065686	.0009508	-6.908	0.000	00846490046722	2		
foreign	-1.627584	1.356207	-1.200	0.234	-4.332454 1.077285	5		
_cons	41.97704	11.02088	3.809	0.000	19.99658 63.9575	5		

If you use expressions in estimation commands, you may benefit from the more readable output of the parameter estimates that is yielded by the command diest, see Weesie (1996).

. diest

mpg	Mileage (mpg)	Coef.	Std. Err.	 t	P> t
weight		0419323 0065686 -1.627584 41.97704	.0009508	-6.908 -1.200	0.978 0.000 0.234 0.000

When using expr, one can still use Stata's post-estimation commands such as predict, test, fit, and so on. For instance,

. predict res, res . test \_Expr0 ( 1) \_Expr0 = 0.0 F( 1, 70) = 0.00 Prob > F = 0.9781

If one wants to use expression expansion interactively for a long series of commands, it may become tedious to type the prefix expr : before all commands. The command exprcmd "switches on" expression expansion in all subsequent commands that are entered interactively. To indicate that expression expansion is on, the command prompt is modified from Stata's period (.) to the string "(expr) .". Thus, the example session shown before could also be entered as

. exprcmd
(expr) . summ price ln(price) weight ln(weight)
(expr) . reg mpg ln(price) weight foreign

Since expression expansion is only supported in "regular commands," you may want to suppress expansion in some commands, for example set, recode, and so on. This is achieved simply by prefixing a command with a period (.), for example

(expr) . .set more off

Finally, interrupting a command with the Break key terminates the command, it does *not* terminate expression expansion. To terminate expansion, one should enter the command (.), i.e., a period.

## References

Weesie, Jeroen. 1996. sg60: Enhancements for the display of estimation results. Stata Technical Bulletin 33: 12-15.

	sbe17	Discrete time prop	ortional ha	zards reg	gression		
_	a 1		1 0		a a:	 	 

Stephen P. Jenkins, ESRC Research Centre on Micro-Social Change, University of Essex, UK, stephenj@essex.ac.uk

Hazard rate models are widely used to model duration data in a wide range of disciplines, from biostatistics to economics. The aim of this insert is to supplement the portfolio of duration data analysis tools which Stata provides.

pgmhaz estimates, by maximum likelihood, two discrete time (grouped duration data) proportional hazards regression models, one of which incorporates a gamma mixture distribution to summarize unobserved individual heterogeneity (or "frailty"). Covariates may include regressor variables summarizing observed differences between persons (either fixed or time-varying), and variables summarizing the duration dependence of the hazard rate. With a suitable definition of covariates, models with a fully nonparametric specification for duration dependence may be estimated; so too may parametric specifications. pgmhaz thus provides a useful complement to cox and st stcox, weibull and st stweib.

The two models estimated are: (1) the Prentice–Gloeckler (1978) model; and (2) the Prentice–Gloeckler (1978) model incorporating a gamma mixture distribution to summarize unobserved individual heterogeneity, as proposed by Meyer (1990). These are referred to as Model 1 and Model 2 respectively below. My exposition of the models draws heavily on that of Stewart (1996).

#### The models

Suppose there are individuals i = 1, ..., n, who each enter a state (e.g. unemployment) at time t = 0. The instantaneous hazard rate function for person i at time t > 0 is assumed to take the proportional hazards form

$$\lambda_{it} = \lambda_0(t) \exp(X_{it}^{\prime}\beta) \tag{1}$$

where  $\lambda_0(t)$  is the baseline hazard function,  $\beta$  is a vector of parameters to be estimated, and  $X_{it}$  is a vector of covariates summarizing observed differences between individuals at t. Let  $\mathbf{X}_{it}$  represent the path of the covariate vector between time 0 and time t.

The underlying continuous durations are only observed in disjoint time intervals  $[0 = a_0, a_1), [a_1, a_2), [a_2, a_3), \dots, [a_{k-1}, a_k = \infty)$ . (Alternatively durations are intrinsically discrete.) Assume that any time-dependent covariates only vary between duration intervals but not within them, i.e. they follow a piece-wise constant (step function) path over time. Thus, letting  $a_t = t, X_{it}$  is constant within each duration interval  $[a_{t-1}, a_t)$ .

The continuous-time survivor function is given by

$$S(t; \mathbf{X}_{it}) = \exp\left[-\sum_{j=a_1}^{a_t} \exp[X'_{ij}\beta + \gamma_j]\right], \text{ where } \gamma_j \equiv \log\int_{a_{j-1}}^{a_j} \lambda_0(\tau)d\tau$$
(2)

If there are no time-varying covariates ( $X_{it} \equiv X_i$ , for all t), (2) simplifies to

.

$$S(t; X_i) = \exp\left\{-\exp\left[X_i\beta + \log(H_t)\right]\right\}$$
(3)

where  $H_t \equiv \int_0^t \lambda_0(\tau) d\tau$  is the integrated baseline hazard at t.

The probability of exit in the jth interval for person i is

$$\Pr\{T \in [a_{j-1}, a_j)\} = S(a_{j-1}; \mathbf{X}_{ij-1}) - S(a_j; \mathbf{X}_{ij})$$

and the survivor function at the start of the jth interval is

$$\Pr\{T \ge a_{j-1}\} = S(a_{j-1}; \mathbf{X}_{ij-1})$$

The hazard of exit in the jth interval is thus given by

$$h_j(X_{it}) \equiv \Pr\{T \in [a_{j-1}, a_j) \mid T \ge a_{j-1}\} = 1 - [S(a_j; \mathbf{X}_{ij}) / S(a_{j-1}; \mathbf{X}_{ij-1})]$$

If there are no time-varying covariates, the discrete-time survivor function has exactly the same form as (3):

$$S(a_j; X_i) = \exp\left\{-\exp\left[X_i'\beta + \delta_j
ight]
ight\}$$
 where  $\delta_j = \log(H_{a_j})$  for  $j = 1, \dots, k$ 

To simplify, let us now suppose that all intervals are of unit length (e.g. a week, or a month), so the recorded duration for each person *i* corresponds to the interval  $[t_i - 1, t_i)$ . Persons are also recorded as either having left the state during the interval, or as still remaining in the state. The former group, contributing completed spell data, are identified using the censoring indicator  $c_i = 1$ . For the latter group, contributing right-censored spell data,  $c_i = 0$ . Observe that the number of intervals comprising a censored spell is defined here to include the last interval within which the person is observed.

The sample log-likelihood can be written

$$\log L(\beta, \delta) = \sum_{i=1}^{n} \left\{ c_i \log[S(t_i - 1; \mathbf{X}_{it_i - 1}) - S(t_i; \mathbf{X}_{it_i})] - (1 - c_i) \log S(t_i; \mathbf{X}_{it_i}) \right\}$$

This expression can be rewritten in terms of the hazard function as

$$\log L = \sum_{i=1}^{n} \left\{ c_i \log \left\{ h_{t_i}(X_{it_i}) \prod_{s=1}^{t_i-1} [1 - h_s(X_{is})] \right\} + (1 - c_i) \log \left\{ \prod_{s=1}^{t_i} [1 - h_s(X_{is})] \right\} \right\}$$

where the discrete-time hazard in the *j*th interval is

$$h_j(X_{ij}) = 1 - \exp[-\exp(X'_{ij}\beta + \gamma_j)]$$

This specification allows for a fully nonparametric baseline hazard with a separate parameter,  $\gamma_j$ , for each duration interval, which can be interpreted as the logarithm of the integral of the baseline hazard over the relevant interval. Alternatively, the sequence of the  $\gamma_j$  may be described by some semiparametric or parametric function.

If one defines an indicator variable  $y_{it} = 1$  if person *i* exits the state during the interval [t - 1, t),  $y_{it} = 0$  otherwise, then the log likelihood can be rewritten in sequential binary response form:

$$\log L = \sum_{i=1}^{n} \sum_{j=1}^{t_i} \{y_{ij} \log h_j(X_{ij}) + (1 - y_{ij}) \log[1 - h_j(X_{ij})]\}$$

This is the version of the Model 1 log likelihood which is estimated by pgmhaz.

Model 2 incorporates a gamma-distributed random variable to describe unobserved heterogeneity between individuals. For a discussion of, and comparison with, other types of mixed proportional hazards models, see Stewart (1996).

The instantaneous hazard rate is now specified as (cf. (1))

$$\lambda_{it} = \lambda_0(t)\varepsilon_i \exp(X_{it}) = \lambda_0(t)\exp[X_{it} + \log(\varepsilon_i)]$$

where  $\varepsilon_i$  is a gamma-distributed random variate with unit mean and variance  $\sigma^2 \equiv v$ , and the corresponding discrete-time hazard function is now

$$h_j(X_{ij}) = 1 - \exp\{-\exp[X'_{ij}\beta + \gamma_j + \log(\varepsilon_i)]\}.$$

Conveniently, the survivor function for the augmented model has a closed form expression (see Meyer 1990 or Dolton and van der Klaauw 1995, for details), and hence so too does the log likelihood function.

The Model 2 log likelihood function is

$$\log L = \sum_{i=1}^{n} \log \{ (1 - c_i)A_i + c_i B_i \}$$

where

$$\begin{split} A_{i} &= \left[ 1 + v \sum_{j=1}^{t_{i}} \exp\left[X_{ij}'\beta + \theta(j)\right] \right]^{-(1/v)} \\ B_{i} &= \begin{cases} \left[ 1 + v \sum_{j=1}^{t_{i}-1} \exp\left[X_{ij}'\beta + \theta(j)\right] \right]^{-(1/v)} - A_{i}, & \text{if } t_{i} > 1 \\ 1 - A_{i}, & \text{if } t_{i} = 1 \end{cases} \end{split}$$

and  $\theta(j)$  is a function describing duration dependence in the hazard rate, including the nonparametric baseline hazard specification  $(\gamma_j)$ . The functional form for  $\theta(j)$  is chosen by the user and specified by defining appropriate covariates—see below. Model 1's log likelihood function is the limiting case as  $v \to 0$ .

For suitably organized data, the log likelihood function for Model 1 is the same as the log likelihood for a generalized linear model of the binomial family with complementary log-log link: see Allison (1982) or Jenkins (1995). Model 1 is estimated by maximum likelihood using Stata's glm command. Model 2 is estimated using Stata's ml deriv0 command, with starting values taken from Model 1's estimates. Given the potential fragility of models incorporating unobserved heterogeneity, estimates for both models are always reported.

#### Syntax

The syntax of pgmhaz is

```
pgmhaz covariates [if exp] [in range] , id(idvar) dead(deadvar) seq(seqvar)
    [lnvar0(#) eform level(#) nolog trace nocons]
```

## Options

lnvar0(#) specifies the value for  $\ln(v)$  which is used as the starting value in the maximization. The default is -1 (i.e.  $v \simeq 0.37$ ).

eform reports coefficients transformed to relative risk format, i.e.  $\exp(\beta)$  rather than  $\beta$ . Standard errors and confidence intervals are similarly transformed. eform may be specified at estimation or when redisplaying results.

level (#) specifies the significance level, in percent, for confidence intervals of the parameters.

nolog suppresses the iteration logs.

trace reports the current value of the estimated parameters of Model 2 at each iteration; see [R] maximize.

nocons specifies no intercept term in the index function  $X'_{ij}\beta$ .

Saved results include the global macros set by ml post, plus S\_1 which contains the Model 2 log likelihood value at maximum, and S\_2 which contains the Model 1 log likelihood value at maximum.

Estimated coefficients and standard errors may be accessed in the usual way: see [U] 20.5 Accessing coefficients and [R] matrix get.

#### Data organization and mandatory variables

The dataset must be organized before estimation so that, for each person, there are as many data rows as there are time intervals at risk of the event occurring for each person. Given the definitions above, this means  $t_i$  rows for each person i = 1, ..., n. In effect an unbalanced panel data set-up is required. This data organization is closely related to that required for estimation of Cox regression models with time-varying covariates. expand is useful for putting the data in this form: see [R] expand, and the example below. Also see the "data step" discussion in Jenkins (1995).

Three variables must be defined by the user:

id(*idvar*) specifies the variable uniquely identifying each person, *i*.

seq(*seqvar*) is the variable uniquely identifying each interval at risk for each person. For each *i*, *seqvar* is the integer sequence  $1, 2, \ldots, t_i$ .

dead(*deadvar*) summarizes censoring status during each interval at risk, and corresponds to the indicator variable  $y_{it}$  described earlier. If  $c_i = 0$ , *deadvar* = 0 for all  $j = 1, 2, ..., t_i$ ; if  $c_i = 1$ , *deadvar* = 0 for all  $j = 1, 2, ..., t_i - 1$ , and *deadvar* = 1 for  $j = t_i$ .

An example of how to construct these variables is given below.

#### Example

This illustration uses the cancer dataset (cancer.dta) supplied with Stata. The dataset provides information about survival times for 48 participants in a cancer drug trial. Of the 48 people, 28 receive the experimental drug treatment (drug = 1) and 20 receive the control treatment (drug = 0). The participants range in age from 47 to 67 years. We wish to analyze time until death, measured in months. The variable studytim records either the month of their death or the last month that they were known to be alive (the maximum value in the data is 39). The persons known to have died have variable died = 1 (contributing completed duration data); those still alive have died = 0 (contributing censored duration data).

First we use the data and recode drug so that it matches the Manual example:

```
. use cancer
(Patient Survival in Drug Trial)
. replace drug = 0 if drug == 1
(20 real changes made)
. replace drug = 1 if drug > 1
(28 real changes made)
```

To run pgmhaz we must reorganize the dataset and create the mandatory variables. To understand what is going on, look at how the data for the first four people is currently organized, and compare this with their data in the reorganized dataset later on.

. gen id	=_n /* c	reate uni	ique person	n identifie	er */			
. list id studytim died drug age in 1/4								
	id stu	ıdytim	died	drug	age			
1.	1	1	1	0	61			
2.	2	1	1	0	65			
з.	3	2	1	0	59			
4.	4	3	1	0	52			

Now expand the dataset so that there is one data row per person per month at risk of dying, and create sequar and dead:

. expand studytim
(696 observations created)
. sort id
. quietly by id: gen seqvar = \_n
. quietly by id: gen dead = died & \_n==\_N

Compare this data format with the earlier one, taking the same four persons:

list	id study	tim seqvar	died dead	age if id	<= 4	
	id	studytim	seqvar	died	dead	age
1.	1	1	1	1	1	61
2.	2	1	1	1	1	65
з.	3	2	1	1	0	59
4.	3	2	2	1	1	59
5.	4	3	1	1	0	52
6.	4	3	2	1	0	52
7.	4	3	3	1	1	52

At this stage, with the data reorganized into person-month form, it would be straightforward to generate time-varying covariates. None are available in cancer.dta however. The illustrative estimations use the fixed covariates drug and age, capturing observed heterogeneity, and use the gamma mixing distribution to capture unobserved heterogeneity.

The first models estimated using pgmhaz assume that duration dependence in the hazard rate is summarized by a parametric "Weibull" specification. This is achieved by including a covariate defined as the logarithm of *seqvar*. (If the estimated coefficient on this regressor is greater than zero, the hazard increases monotonically with duration; if less than zero, it decreases monotonically.) The Model 1 estimates are precisely those which would be produced by the command

. gen logd = ln(seqvar)
. glm deadvar logd drug age, f(b) l(c)

except that in pgmhaz I have added output giving log likelihood values. Incidentally, the logistic hazard counterpart to this proportional hazards model could have been estimated with logit applied to the same reorganized dataset (Allison 1982, Jenkins 1995).

```
. pgmhaz logd drug age, id(id) s(seqvar) d(dead)
(1) PGM hazard model without unobserved heterogeneity
Iteration 1 : deviance = 298.3504
Iteration 2 : deviance = 237.2426
Iteration 3 : deviance = 224.1963
Iteration 4 : deviance = 222.5673
Iteration 5 : deviance = 222.5275
Iteration 6 : deviance = 222.5274
Iteration 7 : deviance = 222.5274
Residual df =
                  740
                                                    No. of obs =
                                                                     744
Pearson X2 = 650.3937
                                                    Deviance = 222.5274
Dispersion = .8789105
                                                    Dispersion = .3007127
Bernoulli distribution, cloglog link
   dead
              Coef. Std. Err.
                                   z P>|z|
                                                    [95% Conf. Interval]
                                 _____
            _ _ _ _ _ _ _ _ _ _ _ _
                     _____
                                          . _ _ _ _ _ _ _ _ _
                                                    _____
   logd
           .6402733 .2448109 2.615 0.009
                                                     .1604526 1.120094
                    .4125618
                               -5.306
                                                    -2.997676 -1.380463
           -2.18907
                                          0.000
   drug
           .119348
                     .0369335
                                3.231
                                          0.001
                                                     .0469596
                                                               .1917364
    age
  _cons -9.928747 2.262543
                                 -4.388 0.000
                                                    -14.36325 -5.494243
            _____
                      _____
                                          _____
   -----
Log likelihood (-0.5*Deviance) = -111.26371
   Cf. log likelihood for intercept-only model (Model 0) = -128.86467
   Chi-squared statistic for Model (1) vs. Model (0) = 35.201924
  Prob. > chi2(3) = 1.104e-07
(2) PGM hazard model with gamma distributed unobserved heterogeneity
Iteration 0: Log Likelihood = -112.22135
Iteration 1: Log Likelihood = -111.09624
Iteration 2: Log Likelihood = -111.08967
Iteration 3: Log Likelihood = -111.08965
Iteration 4: Log Likelihood = -111.08965
PGM hazard model with gamma heterogeneity
                                                Number of obs
                                                                =
                                                                      744
                                                Model chi2(3)
                                                                =
                                                Prob > chi2
Log Likelihood = -111.0896470
```

dead		Std. Err.		P> z	[95% Conf.	Interval]		
hazard								
logd	.8664734	.4787207	1.810	0.070	071802	1.804749		
drug	-2.578879	.8275313	-3.116	0.002	-4.200811	9569476		
age	.141193	.0569466	2.479	0.013	.0295798	.2528062		
_cons	-11.29142	3.510489	-3.216	0.001	-18.17185	-4.410984		
ln_varg								
_cons	-1.247006	1.845572	-0.676	0.499	-4.864262	2.370249		
Gamma variance, exp(ln_varg) = .28736375; Std. Err. = .53035058; z = .54183734								
Likelihood ratio statistic for testing models (1) vs (2) = .34812954 Prob. test statistic > chi2(1) = .55517386								

Comparing pgmhaz Model 1 and Model 2 estimates, we see that the duration dependence parameter is larger in the latter. Moreover, the coefficients in Model 2 on drug and age are slightly larger in absolute value. These differences are not unexpected: not accounting for unobserved heterogeneity induces an underestimate of the extent to which the hazard rate increases with duration (or an overestimate of the decline) and attenuates the magnitude of the impact of covariates on the hazard rate (see Lancaster 1990, chapter 4).

The size of the variance of the gamma mixture distribution relative to its standard error suggests, however, that unobserved heterogeneity is not significant in this dataset. A likelihood ratio test of Model 2 versus Model 1 also suggests the same conclusion. Users should be aware though that standard likelihood ratio tests cannot, strictly speaking, be used to choose between Models 1 and 2, because the former is not a nested version of the latter.

The discrete-time "Weibull" estimates can be compared with the estimates of a continuous-time Weibull model derived using stweib:

```
. stset sequar dead, id(id)
note: making entry-time variable t0
     (within id, t0 will be 0 for the 1st observation and the
     lagged value of exit time sequar thereafter)
  data set name: cancer.dta
          id: id
    entry time: t0
     exit time: sequar
 failure/censor: dead
. stweib drug age, nohr
(output omitted)
Weibull regression -- entry time t0
log relative hazard form
No. of subjects =
                     48
                                       Log likelihood = -42.931336
                    31
No. of failures =
                                       chi2(2)
                                                =
                                                      35.39
                    744
                                       Prob > chi2
                                                        0.0000
Time at risk =
                                                  =
_____
                                   _____
 seqvar | Coef. Std. Err. z P>|z|
                                            [95% Conf. Interval]
 ------
   drug | -2.197157 .408785 -5.375 0.000 -2.998361 -1.395953
                                         .0473823
-15.1433
  age | .1202128 .0371591 3.235 0.001
_cons | -10.58395 2.326241 -4.550 0.000
                                                      .1930433
                                                     -6.024599
                                   _____
  _____
                                            _____
                                                     _____
   ln p | .5203303
                 .1389099 3.746 0.000
                                         .2480718
                                                     .7925887
    р
         1.682583
                                             1.281552
                                                       2.209108
                                             .4526714
   1/p |
         .5943242
                                                      .7803039
```

As it happens, the coefficient estimates are very similar to corresponding estimates in the discrete time "Weibull" model without unobserved heterogeneity. The duration dependence parameters are similar too: compare 1 - p = 0.683 with the coefficient on logd, 0.640.

We should be wary about drawing conclusions about duration dependence from parametric models like the "Weibull" which tightly constrain the shape of the baseline hazard function, when in fact the hazard may vary nonmonotonically with duration. Moreover it is well known that conclusions about the importance of unobserved heterogeneity are more reliably drawn if a flexible specification for the baseline hazard has been used; for a recent discussion, see Dolton and van der Klaauw (1995). Let us therefore compare some models which allow for more flexibility in the shape of the baseline hazard function. One obvious reference point is the continuous time Cox model. Estimates for this are reported in *Stata Reference Manual*, vol. 3, p. 257, and can be reproduced with the command:

. stcox dr	ug age, nohr	baseh(coxbas	eh)			
(output omitte	ed)					
Cox regres	sion entr	y time tO				
No. of sub	jects =	48		Log	likelihood =	-83.323546
No. of fai	lures =	31		chi	2(2) =	33.18
Time at ri	sk =	744		Prol	> chi2 =	0.0000
seqvar   dead	Coef.		z	P> z	[95% Conf.	Interval]
drug   age	-2.254965 .1136186	.4548338 .0372848	-4.958 3.047	0.000 0.002	-3.146423 .0405416	

The Cox baseline hazard function is graphed on p. 279 of *Stata Reference Manual*, *Release 4.0*, vol. 2, and the figure suggests that the hazard increases nonmonotonically with duration. (The picture can be reproduced with the command gr coxbaseh studytim, xlab ylab.) The estimates of the baseline hazard estimate are as follows, and confirm the nonmonotonicity:

. sort	seqvar	
. list	seqvar co	xbaseh if coxbaseh~=.
	seqvar	coxbaseh
16.	1	.00013425
46.	1	.00013425
70.	2	.00007571
112.	3	.00007924
149.	4	.00018067
151.	4	.00018067
196.	5	.0002276
201.	5	.0002276
253.	6	.00026013
255.	6	.00026013
301.	7	.00013608
306.	8	.00044866
307.	8	.00044866
335.	8	.00044866
380.	10	.0001891
404.	11	.00041499
429.	11	.00041499
433.	12	.00056331
435.	12	.00056331
476.	13	.00035089
526.	15	.00038132
532.	16	.00043044
559.	17	.00047959
639.	22	.00149966
641.	22	.00149966
652.	23	.00249846
662.	23	.00249846
672.	24	.00168347
680.	25	.00189012
705.	28	.00228993
734.	33	.00437874

Let us now compare the Cox model estimates with various discrete time proportional hazard model specifications. One example of a flexible parametric specification for the baseline hazard function is a polynomial in duration. One could

```
. gen seqvar_2 = seqvar^2
. gen seqvar_3 = seqvar^3
```

and include seqvar, seqvar\_2, and seqvar\_3, as covariates instead of logd in order to specify a cubic baseline hazard function.

pgmhaz also allows the estimation of fully nonparametric specifications for the baseline hazard (analogously to the Cox model). The duration interval-specific baseline hazard can only be identified for those intervals during which events ('deaths') occur, i.e. values of seqvar for which there are observations (person-months) with dead = 1. If there are intervals for which this is not true,

then either one must change the baseline hazard function specification, or one must drop the relevant person-month observations from the estimation. (see also the discussion of identification of the logit model in *Stata Reference Manual*, vol. 2, pp. 371–375.)

To estimate the nonparametric baseline model, first one has to create binary dummy variables corresponding to each duration interval. It is the user's responsibility to do this and also to check identifiability. This is straightforward. We can create interval-specific dichotomous variables, one for each spell month at risk (the maximum number is 39 here), with the following command:

. quietly for 1-39, ltype(numeric): gen byte d@ = seqvar== @

Next we check identifiability of the baseline hazard at each duration interval with

. tab seqvar	dead dead		
seqvar	0	1	Total
1	46	2	48
2	45	1	46
3	44	1	45
4	42	2	44
5	40	2	42
6	38	2	40
7	36	1	37
8	33	3	36
9	32	0	32
10	30	1	31
11	27	2	29
12	24	2	26
13	23	1	24
14	23	0	23
15	22	1	23
16	20	1	21
17	19	1	20
18	18	0	18
19	18 16	0	18
20 21	15	0	16 15
21	15	2	15
22	13	2	13
23	10	1	13
24	9	1	10
26	8	0	8
20	8	0	8
28	7	1	8
29	6	0	6
30	6	0	6
31	6	0	6
32	6	0	6
33	3	1	4
34	3	0	3
35	2	0	2
36	1	0	1
37	1	0	1
38	1	0	1
39	1	0	1
Total	713	31	744

There are no deaths during months 9, 14, 18–21, 26, 27, 29–32, 34–39, and so a month-specific hazard rate cannot be estimated for these intervals.

The nonparametric baseline model is estimated by including all the relevant duration interval dichotomous variables, excluding observations to ensure identifiability (if necessary), and excluding the intercept using the nocons option. (An alternative estimation strategy would be to include the intercept term and exclude one of the duration interval dichotomous variables.)

. pgmhaz d1-d8 d10-d13 d15-d17 d22-d25 d28 d33 drug age > if (seqvar>=1 & seqvar<=8) | (seqvar>=10 & seqvar<=13) > | (seqvar>=15 & seqvar<=17) | (seqvar>=22 & seqvar<=25) > | seqvar==28 | seqvar==33 , > i(id) s(seqvar) d(dead) nocons (1) PGM hazard model without unobserved heterogeneity

Iteration Iteration Iteration Iteration Iteration Iteration	<pre>1 : deviance 2 : deviance 3 : deviance 4 : deviance 5 : deviance 6 : deviance 7 : deviance 8 : deviance 8 : deviance</pre>	= 206.7409 = 195.2580 = 193.6490 = 193.5947 = 193.5944 = 193.5943 = 193.5943			No. of obs =	573	
Pearson X2 Dispersion					Deviance = Dispersion =		
-	distribution		lr		Dispersion -	.0010007	
dead	Coef.	Std. Err.	z	P> z	[95% Conf.	Interval]	
d1	-9.321505	2.325432	-4.009	0.000	-13.87927	-4.763742	
d2		2.408603	-4.105	0.000	-14.60897	-5.167421	
d3	-9.841984	2.411291	-4.082	0.000	-14.56803	-5.115941	
d4		2.296365	-3.923	0.000	-13.50892	-4.507338	
d5		2.240112	-3.910	0.000	-13.14934	-4.368267	
d6		2.211921	-3.896	0.000	-12.95292	-4.28235	
d7 d8		2.31374 2.152716	-4.006 -3.751	0.000 0.000	-13.80473 -12.29471	-4.735034 -3.856216	
d10		2.322521	-3.846	0.000	-13.4839	-4.379788	
d10 d11		2.201254	-3.700	0.000	-12.45935	-3.830592	
d12		2.202429	-3.550	0.000	-12.13624	-3.502872	
d13		2.282109	-3.626	0.000	-12.74799	-3.802288	
d15		2.265841	-3.615	0.000	-12.63105	-3.749113	
d16	-8.068544	2.291659	-3.521	0.000	-12.56011	-3.576975	
d17	-7.959319	2.257287	-3.526	0.000	-12.38352	-3.535118	
d22	-6.799641	2.161635	-3.146	0.002	-11.03637	-2.562914	
d23		2.12435	-2.933	0.003	-10.39488	-2.067578	
d24		2.287659	-2.884	0.004	-11.0814	-2.11394	
d25		2.285573	-2.836	0.005	-10.96132	-2.002038	
d28		2.302273	-2.734	0.006	-10.80569	-1.780946	
d33		2.350609	-2.405	0.016	-10.26131	-1.04709	
drug		.4668781 .037461	-5.259 3.227	0.000 0.001	-3.370214	-1.540086	
age	.1200959	.037401	3.221		.0474738	.194318	
<pre>Log likelihood (-0.5*Deviance) = -96.797174 Cf. log likelihood for intercept-only model (Model 0) = -120.56974 Chi-squared statistic for Model (1) vs. Model (0) = 47.545131 Prob. &gt; chi2(22) = .0012454 (2) PGM hazard model with gamma distributed unobserved heterogeneity Iteration 0: Log Likelihood = -97.7371 (nonconcave function encountered) Iteration 1: Log Likelihood = -97.178695 Iteration 2: Log Likelihood = -96.672111 Iteration 3: Log Likelihood = -96.666698 Iteration 4: Log Likelihood = -96.666692 Iteration 5: Log Likelihood = -96.666692</pre>							
PGM hazaro	d model with g	gamma heterog	eneity	N	umber of obs	= 573	
					odel chi2(23)		
Log Likeli	ihood = -96	6666923		Р	rob > chi2	= .	
dead	Coef.	Std. Err.	Z	P> z	[95% Conf.	Interval]	
hazard							
d1	-10.80181	3.943248	-2.739	0.006	-18.53043	-3.073185	
d2		3.896149	-2.902	0.004	-18.94406	-3.671436	
d3		3.875214	-2.902	0.004	-18.84046	-3.649898	
d4		3.703692	-2.795	0.005	-17.61088	-3.092676	
d5		3.504439	-2.851	0.004	-16.86032	-3.12317	
d6		3.385348	-2.890	0.004	-16.41971	-3.14939	
d7		3.437018	-3.034	0.002	-17.16412	-3.691257	
d8 d10		3.290664	-2.794	0.005	-15.64358	-2.744411	
d10 d11		3.344376	-2.993 -2 841	0.003 0.005	-16.56612 -15.533	-3.456411 -2.849666	
d11 d12		3.235603 3.177368	-2.841 -2.776	0.005	-15.533 -15.0483	-2.849666 -2.593245	
d12 d13		3.224425	-2.872	0.008	-15.58168	-2.942165	
d15 d15		3.191924	-2.865	0.004	-15.40154	-2.889424	
					·		

d16   d17   d22   d23   d24   d25   d28   d33	-8.978681 -8.819529 -7.626859 -7.076276 -7.436352 -7.276834 -7.038744 -6.276739	3.134165 3.071867 2.946399 2.946105 3.02082 2.97176 2.933167 2.859726	-2.865 -2.871 -2.589 -2.402 -2.462 -2.449 -2.400 -2.195	0.004 0.004 0.010 0.016 0.014 0.014 0.016 0.028	-15.12153 -14.84028 -13.40169 -12.85053 -13.35705 -13.10138 -12.78765 -11.8817	-2.83583 -2.798779 -1.852023 -1.302017 -1.515653 -1.452292 -1.289843 6717789			
drug	-2.863101	.9693994	-2.953	0.003	-4.763088	9631126			
age   +	.1468383	.0667209	2.201	0.028	.0160677	.2776089			
ln_varg _cons	-1.114756	2.041279	-0.546	0.585	-5.115589	2.886076			
Gamma variance, exp(ln_varg) = .32799525; Std. Err. = .66952971; z = .48988902									
	Likelihood ratio statistic for testing models (1) vs (2) = .26096361								
Prob. test statistic > $chi2(1) = .60945891$									

The results suggest that unobserved heterogeneity is not significant in this context, so our preferred specification is Model 1. Parameter estimates for this model correspond quite closely to the Cox ones. In particular, there is a close match in the pattern of variation of the baseline hazard with duration: compare the duration interval dummy variable coefficient estimates with the Cox model estimates listed earlier. The coefficients on drug and age are each somewhat larger in absolute value in the discrete-time model compared to the Cox model.

The earlier tabulation showed that, even for the months in which there were deaths, the number of deaths was relatively small. A model with a piece-wise constant baseline hazard function is an example of a compromise model which allows some nonparametric flexibility in the duration dependence specification, but may help estimation precision when there are few spell endings per duration interval. To specify a baseline hazard which is constant within six month intervals up to durations of 30 months and constant thereafter, but allowed to vary between these intervals, one would simply

. gen dur1 = d1+d2+d3+d4+d5+d6 . gen dur2 = d7+d8+d9+d10+d11+d12 . gen dur3 = d13+d14+d15+d16+d17+d18 . gen dur4 = d19+d20+d21+d22+d23+d24 . gen dur5 = d25+d26+d27+d28+d29+d30 . gen dur6 = d31+d32+d33+d34+d35+d36+d37+d38+d39

and use the command

. pgmhaz dur1-dur6 drug age, i(id) s(seqvar) d(dead) nocons

Estimates of Models 1 and 2 for this case (not shown here) indicate that unobserved heterogeneity is not significant and there is again evidence of a nonmonotonic increase in the baseline hazard with duration. The coefficients on age and drug are similar to those estimated by both the Cox model and the discrete time proportional hazards model with nonparametric baseline hazard.

#### Computational and other issues

pgmhaz can be slow, or rather estimation of Model 2 can be. This is partly because the maximization procedure uses numerical derivatives, and also partly because reorganized datasets can be relatively "large". Models with fully nonparametric baseline hazard function specifications also take significantly longer to estimate than models with parsimonious parametric specifications. Using a Pentium P-120 "smrm PC with 32MB RAM and Stata 5.0 for Windows 3.11 for Workgroups, the "Weibull" pgmhaz model took about one minute to run, and the nonparametric baseline hazard model about seven minutes. Using a different dataset from cancer.dta, one with 7410 person-month observations, a model with one covariate and thirteen duration interval dummy variables took about 30 minutes to complete.

The log likelihood function for Model 2 is not globally concave, but convergence is usually achieved without problems. If there are maximization difficulties, users may find the trace option useful for diagnosing problems. Setting different starting values for the logarithm of the gamma variance with the lnvar0(#) option may also be helpful.

A warning. Because of the particular ordered sequence person-month structure of the data, the *if* option should be used with great care (and the *in* option should probably never be used). An *if* expression which refers to all the data rows for each person will be handled correctly, e.g., selection of an estimation sub-sample according to values of a fixed covariate. Do not select cases using an expression referring to a duration-varying variable or the results may be unpredictable. One exception to this rule arises when some observations need to be excluded to ensure identifiability of a model with a nonparametric baseline hazard function, as illustrated

earlier. (In this context, there is one situation I am aware of in which the program will be incorrect if this strategy is followed. This is when the data contain a person contributing s > 1 intervals to the analysis who "dies" in the *s*th interval, and there are no "deaths" observed for any person in the sample during any of the duration intervals prior to *s*. This situation is likely to be rare.)

#### Acknowledgments

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sg72	Newey–West standard errors for probit, logit, and poisson models

James W. Hardin, Stata Corporation, stata@stata.com

This article discusses the calculation of standard errors that are robust to heteroscedasticity and serial correlation for probit, logit, and poisson regression models.

In order to calculate any statistic dealing with serial correlation, one must have a variable that identifies the time at which the individual observations were collected. This is to ensure that the observations are placed in the correct order and that the time steps between observations are constant so that the lag-dependent calculations are done correctly.

## Methods and formulas

In this article, we focus on a model which may be written as  $y_t = m_t(\mathbf{x}_t, \beta)$  where  $m_t$  is the conditional mean of  $y_t$  given the covariates  $\mathbf{x}_t$ . We also introduce a parametric family of weighting functions to be used in weighted nonlinear least squares (WNLS) estimation such that the weighting function  $h_t(\mathbf{x}_t, \gamma)$  is strictly positive. The motivation of the weighting function is that for some value of  $\gamma$ , the weight function is proportional to the conditional variance of  $y_t$  given the covariates  $\mathbf{x}_t$  and the WNLS estimator  $\hat{\beta}$  is then given by the value of  $\beta$  minimizing

$$\sum_{t=1}^{T} (y_t - m_t(\mathbf{x}_t - \beta))^2 / h_t(\mathbf{x}_t, \widehat{\gamma})$$

such that under the hypothesis that the conditional mean function is correct, the estimator is asymptotically normal with variance of the form  $A^{-1}BA^{-1}$ . We can then estimate the variance using

$$\widehat{\mathbf{A}} = \frac{1}{T} \sum_{t=1}^{T} \widehat{g}_t^2$$

$$\widehat{\mathbf{B}} = \widehat{\Omega}_0 + \sum_{j=1}^{G} \omega(j) \left\{ \widehat{\Omega}_j + \widehat{\Omega}'_j \right\}$$

$$\widehat{\Omega}_j = \frac{1}{T} \sum_{i=j+1}^{T} \widehat{s}_i \widehat{s}_{t-j}$$

$$\omega(j) = 1 - j/(G+1)$$

where  $\hat{g}_t$  is the weighted gradient (evaluated at  $\hat{\beta}$ ),  $\hat{s}_t$  is the weighted residual, and G is the maximum lag to consider (the bandwidth). Note that under the hypothesis of independent observations (G = 0), we would have the usual White estimate of variance (c.f. the example of linear regression). Newey and West (1987) show that  $\widehat{\mathbf{B}}$  is positive semi-definite. Other extensions of this approach that use a different weight function  $\omega(j)$  and bandwidth G are not included in this command.

For details on the theoretical derivation of these estimators, the interested reader should consult Wooldridge (1991) or Hamilton (1994), especially chapter 10.

## Syntax

The syntax for nwest is

```
nwest command varlist [if exp] [in range] [, lag(#) <u>level(#)</u> t(varname<sub>t</sub>) opts ]
```

where *command* is one of regress, logit, probit, or poisson.

Note that nwest regress will produce the same results as using Stata's newey command.

## Options

lag(#) specifies the maximum lag to consider in calculating the standard errors. The default is zero.

- level(#) specifies the confidence level, in percent, for confidence intervals. The default is level(95) or as set by set level; see
  [U] 26.4 Specifying the width of confidence intervals.
- t(varname<sub>t</sub>) needs to be specified only if a nonzero lag() is also specified; t() specifies the variable that contains the time at which each observation was recorded. t() can also be omitted if it has been specified on a previous run; nwest will remember the previous identity of t().

opts are options supported by the individual command (e.g., irr for poisson).

#### Example: linear regression models

We use the automobile dataset to illustrate that the nwest command will produce the same results as the newey command. We also show that considering the Newey–West estimate with lag zero is equivalent to the robust standard error provided by the regress command.

. nwest re	gress price w	veight displ						
Regression	Regression with Newey-West standard errors Number of obs = 74							
maximum la	g:0				F(2, 71) =	14.44		
					Prob > F =	0.0000		
		Newey-West						
price	Coef.	Std. Err.	t	P> t	[95% Conf.	Interval]		
weight	1.823366	.7808755	2.335	0.022	.2663446	3.380387		
displ	2.087054	7.436967	0.281	0.780	-12.74184	16.91595		
_cons	247.907	1129.602	0.219	0.827	-2004.454	2500.269		
. newey pr	ice weight d	ispl, lag(0)						
Regression	with Newey-W	lest standard	errors		Number of obs =	74		
maximum la	g:0				F(2, 71) =	14.44		
	•				Prob > F =	0.0000		
		Newey-West						
price	Coef.	Std. Err.	t	P> t	[95% Conf.	Interval]		
weight	1.823366	.7808755	2.335	0.022	.2663446	3.380387		
displ	2.087054	7.436967	0.281	0.780	-12.74184	16.91595		
_cons	247.907	1129.602	0.219	0.827	-2004.454	2500.269		

. regress price weight displ, robust

Regression	with robust	standard err	ors		Number of obs F(2,71) Prob > F R-squared Root MSE	
price	Coef.	Robust Std. Err.	t	P> t	[95% Conf.	Interval]
weight   displ   _cons	1.823366 2.087054 247.907	.7808755 7.436967 1129.602	2.335 0.281 0.219	0.022 0.780 0.827	.2663446 -12.74184 -2004.454	3.380387 16.91595 2500.269

## Example: probit and logit models

In this example, we use data on the unionization of women. We first present the results of a probit analysis not addressing possible heteroscedasticity or serial correlation.

. probit un	ion age grad	le not_smsa s	outh south	nXt		
Iteration 1 Iteration 2	: Log Like] : Log Like]	Lihood =-1046 Lihood =-1025 Lihood =-1025	2.844 2.282			
Iteration 3: Log Likelihood =-10252.282 Probit Estimates Log Likelihood = -10252.282					Number of obs = 19224 chi2(5) = 426.87 Prob > chi2 = 0.0000 Pseudo R2 = 0.0204	
 union	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
grade   not_smsa   south	.0188945 1474075 3319289 0002766	.0018991 .0042971 .0233975 .285638 .0035351 .0793062	4.397 -6.300 -1.162 -0.078	0.002 0.000 0.000 0.245 0.938 0.000	.0104724 .0273167 19326581015493 891769 .2279113 0072052 .0066521	

As there are repeated observations over time, we suspect that there will be a problem with serial correlation which should be addressed (up to lag 2).

. nwest probit union age grade not_smsa south southXt, $lag(2)$ t(time)									
Probit with	Probit with Newey-West standard errors Number of obs = 19224								
maximum lag	;:2				chi2( 5) =	227.09			
-					Prob > chi2 =	0.0000			
1		Newey-West							
union	Coef.	Std. Err.	z	P> z	[95% Conf.	Interval]			
+-									
age	.0058862	.0024516	2.401	0.016	.0010811	.0106912			
grade	.0188945	.0063701	2.966	0.003	.0064093	.0313798			
not_smsa	1474075	.0318795	-4.624	0.000	2098902	0849249			
south	3319289	.3573839	-0.929	0.353	-1.032389	.3685308			
southXt	0002766	.0044246	-0.063	0.950	0089486	.0083954			
_cons	9784501	.1103485	-8.867	0.000	-1.194729	7621709			

Note that probit and logit models may be run the same way using the logit keyword instead of the probit keyword.

## Example: poisson models

In this example, we use the data listed in the Stata Reference Manual:

. list

	agecat	smokes	deaths	pyears
1.	1	1	32	52407
2.	2	1	104	43248
з.	3	1	206	28612
4.	4	1	186	12663
5.	5	1	102	5317

6.	1	0	2	18790
7.	2	0	12	10673
8.	3	0	28	5710
9.	4	0	28	2585
10.	5	0	31	1462

We would like to obtain the robust standard errors but the poisson command does not have a robust option. We also can not obtain robust standard errors from the glm command as it does not have the robust option either.

tah arec	at, gen(a)					
ageca		q. Percen	t C	Cum.		
	1	2 20.0	0 20	.00		
	2	2 20.0		.00		
	3	2 20.0	0 60	0.00		
	4	2 20.0	0 80	0.00		
	5	2 20.0	0 100	0.00		
Tota	.1   1	100.0	0			
poisson	deaths smokes	s a2-a5, expo	sure(pyear	rs) irr		
teration	0: Log Likeli	ihood = -34.0	22705			
	1: Log Likeli					
teration	2: Log Likeli	ihood = -33.6	00098			
		= 12 = 0.	years .132 0164 .600		Number of obs Model chi2(5) Prob > chi2 Pseudo R2	= 10 = 922.935 = 0.0000 = 0.9321
deaths	IRR	Std. Err.	z	P> z	[95% Conf.	Interval]
smokes	1.425518	.1530638	3.302	0.001	1.154984	1.759421
a2	4.410583	.8605195	7.606	0.000	3.009011	6.464996
a3	13.8392	2.542637	14.301	0.000	9.654325	19.83809
a4	28.51678	5.269876	18.130	0.000	19.85177	40.96395
a5	40.4512	7.77551	19.249	0.000	27.75325	58.95888
nwest po	isson deaths	smokes a2-a5	, exposure	(pyear:	s) irr	
=	th Newey-West.		=	e(pyears	s) irr Number of obs = chi2(5) = Prob > chi2 =	
oisson wi	th Newey-West.		=	(pyear:	Number of obs = chi2(5) =	7089.45
oisson wi	th Newey-West.	standard er	=	e(pyears P> z	Number of obs = chi2(5) =	7089.48 0.0000
Poisson wi naximum la 	th Newey-West g : O	standard er Robust	rors		Number of obs = chi2(5) = Prob > chi2 =	7089.45 0.0000 Interval
oisson wi aximum la 	th Newey-West g : 0 IRR	t standard er Robust Std. Err.	rors z	P> z	Number of obs = chi2(5) = Prob > chi2 = [95% Conf.	7089.45 0.0000 Interval
oisson wi aximum la deaths   smokes	th Newey-West g : 0 IRR 1.425518	Robust Std. Err. .1665546	rors z 3.034	P> z  0.002	Number of obs = chi2(5) = Prob > chi2 = [95% Conf. 1.133758	7089.48 0.0000 Interval 1.792363 6.654468
Poisson vi naximum la deaths   smokes   a2	th Newey-West g : 0 IRR 1.425518 4.410583	Robust Std. Err. .1665546 .9255229	z 3.034 7.072	P> z  0.002 0.000	Number of obs = chi2(5) = Prob > chi2 = [95% Conf. 1.133758 2.923335	7089.45 0.0000

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dm	data management		interprogram communication			
dt	datasets	qs	questions and suggestions			
gr	graphics	tt	teaching			
in	instruction	ZZ	not elsewhere classified			
Statistical Categories:						
sbe	biostatistics & epidemiology	ssa	survival analysis			
sed	exploratory data analysis	ssi	simulation & random numbers			
sg	general statistics	SSS	social science & psychometrics			
smv	multivariate analysis	sts	time-series, econometrics			
snp	nonparametric methods	svy	survey sampling			
sqc	quality control	sxd	experimental design			
sqv	analysis of qualitative variables	SZZ	not elsewhere classified			
srd	robust methods & statistical diagnostics					

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Fax:	+49 212-3390 200 +49 212-3390 295	Fax:	+61 3 59788623
Email:	evhall@dpc.de	Email:	rosier@survey-design.com.au
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